## ETC4500/ETC5450 Advanced R programming

Week 1: Foundations of R programming
arp.numbat.space


## Outline

## 1 Introduction to R

2 Names and values

## 3 Vectors

## First things first

## Expectations

- You know R and RStudio
- You have a basic understanding of programming (for loops, if statements, functions)
- You can use Git and GitHub (https://happygitwithr.com)


## Unit resources

■ Everything on https://arp.numbat.space

- Assignments submitted on Github Classroom
- Discussion on Ed


## GitHub

- Use your monash edu address.

■ Apply to GitHub Global Campus as a student (https://education.github.com).

- Gives you free access to private repos and GitHub Copilot.

■ Add GitHub Copilot to RStudio settings.

## Outline

## 1 Introduction to R

## 2 Names and values

3 Vectors

■ S (1976, Chambers, Becker and Wilks; Bell Labs, USA)
■ S-PLUS (1988, Doug Martin; Uni of Washington, USA)

- R (1993, Ihaka and Gentleman; Uni of Auckland, NZ)


## R history

■ S (1976, Chambers, Becker and Wilks; Bell Labs, USA)
■ S-PLUS (1988, Doug Martin; Uni of Washington, USA)

- R (1993, Ihaka and Gentleman; Uni of Auckland, NZ)


## R influenced by

- Lisp (functional programming, environments, dynamic typing)
- Scheme (functional programming, lexical scoping)
- S and S-PLUS (syntax)


## Why R?

■ Free, open source, and on every major platform.

- A diverse and welcoming community

■ A massive set of packages, often cutting-edge.
■ Powerful communication tools (Shiny, Rmarkdown, quarto)

- RStudio IDE

■ Deep-seated language support for data analysis.

- A strong foundation of functional programming.
- Posit
- Easy connection to high-performance programming languages like C, Fortran, and C++.


## R challenges

■ R users are not usually programmers. Most R code by ordinary users is not very elegant, fast, or easy to understand.
■ R users more focused on results than good software practices.

- R packages are inconsistent in design.
$\square$ R can be slow.


## Outline

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2 Names and values
3 Vectors

## Exercises

1 Given the following data frame, how do I create a new column called " 3 " that contains the sum of 1 and 2 ? You may only use $\$$, not [ [. What makes 1,2 , and 3 challenging as variable names?

```
df <- data.frame(runif(3), runif(3))
names(df) <- c(1, 2)
```

2 In the following code, how much memory does y occupy?

```
x <- runif(1e6)
y <- list(x, x, x)
```

3 On which line does a get copied in the following example?

```
a <- c(1, 5, 3, 2)
b <- a
b[[1]] <- 10
```


## Binding basics

$x<-c(1,2,3)$


■ Creates an object, a vector of values, c(1, 2, 3).
$\square$ Binds that object to a name, x.
$\square$ A name is a reference (or pointer) to a value.

## Binding basics

$x<-c(1,2,3)$


■ Creates an object, a vector of values, c(1, 2, 3).
$\square$ Binds that object to a name, x.
$\square$ A name is a reference (or pointer) to a value.


■ Binds the same object to a new name, y.

## Binding basics

```
library(lobstr)
obj_addr(x)
```

[1] "0x55baa524b958"
obj_addr (y)
[1] "0x55baa524b958"
These identifiers are long, and change every time you restart R.

## Syntactic names

## A syntactic name:

■ must consist of letters, digits, . and _

- can't begin with _, or a digit, or a . followed by a digit
- can't be a reserved word like TRUE, NULL, if, and function

```
_abc <- 1
#> Error: unexpected input in "_"
if <- 10
#> Error: unexpected assignment in "if <-"
```


## Syntactic names

## A syntactic name:

■ must consist of letters, digits, . and

- can't begin with _, or a digit, or a . followed by a digit
- can't be a reserved word like TRUE, NULL, if, and function

```
_abc <- 1
#> Error: unexpected input in "_"
if <- 10
#> Error: unexpected assignment in "if <-"
```

It's possible to override these rules using backticks.

```
__abc` <- 1
`_abc`
```


## Copy-on-modify

Consider the following code. It binds x and y to the same underlying value, then modifies y .

```
x<-c(1, 2, 3)
y<- x
```



## Copy-on-modify

Consider the following code. It binds $x$ and $y$ to the same underlying value, then modifies y .

```
x<-c(1, 2, 3)
y<- x
```



```
y[[3]] <- 4
x
```

[1] 123


## tracemem()

## You can see when an object gets copied using tracemem().

```
x <- c(1, 2, 3)
tracemem(x)
```

[1] "<0x55baa5128208>"

```
y <- x
y[[3]] <- 4L
```

tracemem[0x55baa5128208 -> 0x55baa1a59798]: eval eval eval_with_user_handlers withVisible wit

```
y[[3]] <- 5L
```

tracemem[0x55baa1a59798 -> 0x55baa4fa0578]: eval eval eval_with_user_handlers withVisible wit

```
untracemem(x)
```


## Modify-in-place

If an object has a single name bound to it, R will modify it in place:
$v<-c(1,2,3)$

$v[[3]]<-4$


## Function calls

The same rules for copying also apply to function calls.

```
f <- function(a) {
    a
}
x <- c(1, 2, 3)
tracemem(x)
```

[1] "<0x55baa4f8ee68>"

```
z <- f(x)
# there's no copy here!
untracemem(x)
```


## Lists

Lists store references to their elements, not the elements themselves.
l1 <- list(1, 2, 3)


## Lists

## Lists store references to their elements, not the elements themselves. <br> ```l1 <- list(1, 2, 3)``` <br> 

l2 <- l1


## Lists

Lists store references to their elements, not the elements themselves.

```
l1 <- list(1, 2, 3)
```



## Data frames



## Data frames



Modifying a column:

```
d2 <- d1
d2[, 2] <- d2[, 2] * 2
```



## Data frames

## Data frames are lists of vectors.

d1 <- data.frame $(x=c(1,5,6), y=c(2,4,3))$


Modifying a row:

```
d3 <- d1
d3[1, ] <- d3[1, ] * 3
```



## Character vectors

x <- c ("a", "a", "abc", "d")

| $x \rightarrow$ | $" a "$ | $" a "$ | $" a b c "$ | $" d "$ |
| :--- | :--- | :--- | :--- | :--- |

■ Not quite!

- R actually uses a global string pool where each element is a pointer to a string in the pool



## Object size

```
lobstr::obj_size() gives the size of an object in memory.
obj_size(ggplot2::diamonds)
3.46 MB
banana <- "bananas bananas bananas"
obj_size(banana)
1 3 6 ~ B
obj_size(rep(banana, 100))
928 B
```


## Object size

```
x <- runif(le6)
obj_size(x)
8.00 MB
y <- list(x, x, x)
obj_size(y)
8.00 MB
obj_size(x, y)
8.00 MB
```


## ALTREP

```
obj_size(1:3)
```


## 680 B

```
obj_size(1:1e6)
```

680 B

```
obj_size(c(1:1e6, 10))
```

8.00 MB

```
obj_size(2 * (1:1e6))
```

8.00 MB

## For loops

## Loops have a reputation for being slow, but often that is caused by iterations creating copies.

```
x <- data.frame(matrix(runif(3 * 1e4), ncol = 3))
medians <- vapply(x, median, numeric(1))
tracemem(x)
for (i in seq_along(medians)) {
    x[[i]] <- x[[i]] - medians[[i]]
}
```

tracemem[0x55baa51f7048 -> 0x55baa5180ca8]: eval eval eval_with_user_handlers withVisible wit tracemem[0x55baa5180ca8 -> 0x55baa5180d98]: [[<-.data.frame [[<- eval eval eval_with_user_han tracemem[0x55baa5180d98 -> 0x55baa5180e38]: eval eval eval_with_user_handlers withVisible wit tracemem[0x55baa5180e38 -> 0x55baa5181018]: [[<-.data.frame [[<- eval eval eval_with_user_han tracemem[0x55baa5181018 -> 0x55baa5181108]: eval eval eval_with_user_handlers withVisible wit tracemem[0x55baa5181108 $\rightarrow$ 0x55baa51811f8]: [[<-.data.frame [[<- eval eval eval_with_user_han

■ Each iteration copies the data frame two times!

## For loops

```
The same problem but with a list.
y <- as.list(x)
tracemem (y)
for (i in 1:3) \{
    \(y[[i]]\) <- y[[i]] - medians[[i]]
\}
```

tracemem[0x55baa516e558 -> 0x55baa51443b8]: eval eval eval_with_user_handlers withVisible wit
■ Only one copy created

## Don't allocate memory in a for loop

```
```


# Allocating memory within the loop

```
```


# Allocating memory within the loop

system.time(
system.time(
{
{
x <- NULL
x <- NULL
for(i in seq(1e5)) {
for(i in seq(1e5)) {
x <- c(x, i)
x <- c(x, i)
}
}
}
}
)

```
```

)

```
```

| user | system | elapsed |
| ---: | ---: | ---: |
| 6.358 | 0.008 | 6.366 |

```
# Allocating memory before the loop
```


# Allocating memory before the loop

system.time(
system.time(
{
{
x <- numeric(1e5)
x <- numeric(1e5)
for(i in seq(1e5)) {
for(i in seq(1e5)) {
x[i] <- i
x[i] <- i
}
}
}
}
)

```
)
```

user system elapsed
0.0060 .0000 .006

## Unbinding and the garbage collector

$x<-1: 3$

| $x \rightarrow 0 \times 74 b$ |
| :---: | :---: | :---: |

## Unbinding and the garbage collector

$$
x<-1: 3
$$



$$
x<-2: 4
$$



## Unbinding and the garbage collector

$$
x<-1: 3
$$

$$
\begin{array}{|l|l|c|}
\hline x & \begin{array}{|l|l|l|}
\hline 1 & 2 & 3 \\
\hline
\end{array} \\
\hline
\end{array}
$$

$$
x<-2: 4
$$


$r m(x)$


## Garbage collection

- Garbage collection (GC) frees up memory by deleting R objects that are no longer used, and by requesting more memory from the operating system if needed.
■ R traces every object that's reachable from the global environment (recursively).
- GC runs automatically whenever R needs more memory to create a new object.
■ You can force garbage collection by calling gc(). But it's never necessary.


## Outline

1 Introduction to R

## 2 Names and values

## 3 Vectors

- Vectors come in two flavours: atomic vectors and lists
- For atomic vectors, all elements must have same type
- For lists, elements can have different types
- nULL is like a generic zero length vector

■ Scalars are just vectors of length 1

- Every vector can also have attributes: a named list of arbitrary metadata.
- The dimension attribute turns vectors into matrices and arrays.
■ The class attribute powers the S3 object system.


## Atomic vectors

■ Four primary types of atomic vectors: logical, integer, double, and character (which contains strings).

- Collectively integer and double vectors are known as numeric vectors

■ Two rare types:

- complex
- raw.



## Scalars

■ Logicals: true or false, or abbreviated (T or F).
■ Doubles: decimal (0.1234), scientific (1.23e4), or hexadecimal (0xcafe). Special values: Inf, -Inf, and NaN (not a number).
■ Integers: 1234L, 1e4L, or 0xcafeL. Can not contain fractional values.

■ Strings: "hi" or 'bye'. Special characters are escaped with $\backslash$.

## Making longer vectors with c()

Use c() to create longer vectors from shorter ones.

```
lgl_var <- c(TRUE, FALSE)
int_var <- c(1L, 6L, 10L)
dbl_var <- c(1, 2.5, 4.5)
chr_var <- c("these are", "some strings")
```

When the inputs are atomic vectors,
 c() always flattens.
$c(c(1,2), c(3,4))$
[1] 1234

## Types and length

You can determine the type of a vector with typeof() and its length with length ().

```
typeof(lgl_var)
```

[1] "logical"
typeof(int_var)
[1] "integer"
typeof(dbl_var)
[1] "double"
typeof(chr_var)
[1] "character"

## Missing values

Most computations involving a missing value will return another missing value.
$\mathrm{NA}>5$
[1] NA
10 * NA
[1] NA
! NA
[1] NA

## Missing values

## Exceptions:

```
NA ^ 0
```

[1] 1
NA | TRUE
[1] TRUE
NA \& FALSE
[1] FALSE

## Missing values

```
Use is.na() to check for missingness
x <- c(NA, 5,NA, 10)
x == NA
```

[1] NA NA NA NA

```
is.na(x)
```

[1] TRUE FALSE TRUE FALSE
There are actually four missing values: NA (logical), NA_integer_ (integer), NA_real_ (double), and NA_character_ (character).

## Coercion

- For atomic vectors, all elements must be the same type.
$\square$ When you combine different types they are coerced in a fixed order: logical $\rightarrow$ integer $\rightarrow$ double $\rightarrow$ character.

```
str(c("a", 1))
    chr [1:2] "a" "1"
x <- c(FALSE, FALSE, TRUE)
as.numeric(x)
```

[1] 001

```
sum(x)
```

[1] 1

```
as.integer(c("1", "1.5", "a"))
```

[1] $1 \quad 1 \mathrm{NA}$

## Exercises

4 Predict the output of the following:

```
c(1, FALSE)
c("a", 1)
c(TRUE, 1L)
```

5 Why is 1 == " 1 " true? Why is -1 < FALSE true? Why is "one" < 2 false?

6 Why is the default missing value, NA, a logical vector? What's special about logical vectors? (Hint: think about c(FALSE, NA_character_).)

## Getting and setting attributes

■ You can think of attributes as name-value pairs that attach metadata to an object.

- Individual attributes can be retrieved and modified with attr(), or retrieved en masse with attributes(), and set en masse with structure().

```
a <- 1:3
attr(a, "x") <- "abcdef"
a
```

[1] 123
attr(,"x")
[1] "abcdef"

## Getting and setting attributes

```
attr(a, "y") <- 4:6
str(attributes(a))
List of 2
\$ x: chr "abcdef"
\$ \(y:\) int [1:3] 456
```

```
# Or equivalently
```


# Or equivalently

a <- structure(
a <- structure(
1:3,
1:3,
x = "abcdef",
x = "abcdef",
y = 4:6
y = 4:6
)
)
str(attributes(a))

```
str(attributes(a))
```


List of 2
\$ x: chr "abcdef"
\$ y: int [1:3] 456

## Names

- Names are a type of attribute.
- You can name a vector in three ways:

```
# When creating it:
x<-c(a=1,b=2,c=3)
# By assigning a character vector to names()
x<- 1:3
names(x) <- c("a", "b", "c")
# Inline, with setNames():
x <- setNames(1:3, c("a", "b", "c"))
```

X

## Names

■ Avoid using attr(x, "names") as it requires more typing and is less readable than names ( $x$ ).
■ You can remove names from a vector by using x <- unname(x) Or names(x) <- NULL.

## Dimensions

- Adding a dim attribute to a vector allows it to behave like a 2-dimensional matrix or a multi-dimensional array.
- You can create matrices and arrays with matrix() and array (), or by using the assignment form of dim():

```
# Two scalar arguments specify row and column sizes
x <- matrix(1:6, nrow = 2, ncol = 3)
```

X
[,1] [,2] [,3]
$[1] \quad 1 \quad 3 \quad$,

| $[2]$, | 2 | 4 | 6 |
| :--- | :--- | :--- | :--- |

## Dimensions

```
# One vector argument to describe all dimensions
y <- array(1:12, c(2, 3, 2))
y
```

, , 1
[,1] [,2] [,3]
$[1] \quad 1 \quad 3 \quad$,
$[2] \quad 2 \quad 4 \quad$,
, , 2

## Dimensions

```
# You can also modify an object in place by setting dim()
z <- 1:6
dim(z) <- c(3, 2)
Z
    [,1] [,2]
    [1,] 1 4
    [2,] 2 5
    [3,] 3 6
```


## Exercises

7 What does dim() return when applied to a 1-dimensional vector?

8 When might you use NROW() or NCOL ()?
9 How would you describe the following three objects? What makes them different from 1:5?

```
x1 <- array(1:5, c(1, 1, 5))
x2 <- array(1:5, c(1, 5, 1))
x3 <- array(1:5, c(5, 1, 1))
```


## S3 atomic vectors

- class is a vector attribute.
- It turns object into S3 object.
- Four important S3 vectors:
- factor vectors.
- Date vectors with day resolution.
- POSIXCt vectors for date-times.
- difftime vectors for durations.



## Factors

- A vector that can contain only predefined values.
- Used to store categorical data.
- Built on top of an integer vector with two attributes: a class, "factor", and levels, which defines the set of allowed values.

```
x
[1] a b b a
Levels: a b
```

x <- factor (c("a", "b", "b", "a"))

## Factors

## typeof(x)

[1] "integer"

## attributes(x)

\$levels

[1] "a" "b"
\$class
[1] "factor"

## Factors

```
sex_char <- c("m", "m", "m")
sex_factor <- factor(sex_char, levels = c("m", "f"))
table(sex_char)
sex_char
m
3
table(sex_factor)
sex_factor
m f
30
```


## Factors

- Be careful: some functions convert factors to integers!
- ggplot preserves ordering of levels in graphs - useful to reorder panels or legends.
- Ordered factors are useful when the order of levels is meaningful.

```
grade <- ordered(c("b", "b", "a", "c"), levels = c("c", "b", "a"))
grade
```

[1] b b a c
Levels: $c<b<a$

## Dates

■ Date vectors are built on top of double vectors.
■ Class "Date" with no other attributes:

```
today <- Sys.Date()
typeof(today)
[1] "double"
attributes(today)
```

\$class
[1] "Date"

## Dates

The value of the double (which can be seen by stripping the class), represents the number of days since 1970-01-01 (the "Unix Epoch").

```
date <- as.Date("1970-02-01")
unclass(date)
```

[1] 31

## Date-times

- Base R provides two ways of storing date-time information, POSIXct, and POSIXlt.
■ "POSIX" is short for Portable Operating System Interface
■ "ct" stands for calendar time; "lt" for local time
$\square$ POSIXct vectors are built on top of double vectors, where the value represents the number of seconds since 1970-01-01.

```
now_ct <- as.POSIXct("2018-08-01 22:00", tz = "UTC")
now_ct
```

[1] "2018-08-01 22:00:00 UTC"

## Date-times

The tzone attribute controls only how the date-time is formatted; it does not control the instant of time represented by the vector. Note that the time is not printed if it is midnight.

```
structure(now_ct, tzone = "Asia/Tokyo")
```

[1] "2018-08-02 07:00:00 JST"

```
structure(now_ct, tzone = "America/New_York")
```

[1] "2018-08-01 18:00:00 EDT"
structure(now_ct, tzone = "Australia/Lord_Howe")
[1] "2018-08-02 08:30:00 +1030"

## Exercises

10
What sort of object does table() return? What is its type? What attributes does it have? How does the dimensionality change as you tabulate more variables?

11 What happens to a factor when you modify its levels?

```
f1 <- factor(letters)
levels(f1) <- rev(levels(f1))
```

What does this code do? How do f2 and f3 differ from f1?

```
f2 <- rev(factor(letters))
f3 <- factor(letters, levels = rev(letters))
```


## Lists

- More complex than atomic vectors
- Elements are references to objects of any type

```
l1 <- list(
    1:3, "a", c(TRUE, FALSE, TRUE), c(2.3, 5.9)
)
typeof(l1)
[1] "list"
str(l1)
List of 4
    $ : int [1:3] 1 2 3
    $ : chr "a"
    $ : logi [1:3] TRUE FALSE TRUE
    $ : num [1:2] 2.3 5.9
```


## Lists

■ Lists can be recursive: a list can contain other lists.

```
l3 <- list(list(list(1)))
```

str(l3)

List of 1
\$ :List of 1
.. $\$$ :List of 1
.. . . $\$$ : num 1


## Lists

## - c() will combine several lists into one.

```
l4 <- list(list(1, 2), c(3, 4))
l5 <- c(list(1, 2), c(3, 4))
str(l4)
```

List of 2
\$ :List of 2
.. $\$$ : num 1
.. $\$$ : num 2
\$ : num [1:2] 34

## str (15)

```
List of 4
    $ : num 1
    $ : num 2
    $ : num 3
    $ : num 4
```


## Testing and coercion

```
list(1:3)
[[1]]
[1] 1 2 3
as.list(1:3)
[[1]]
[1] 1
[[2]]
[1] 2
[[3]]
[1] 3
```

- You can turn a list into an atomic vector with unlist().


## Data frames and tibbles

- Most important S3 vectors built on lists: data frames and tibbles.

```
df1 <- data.frame(x = 1:3, y = letters[1:3])
\$names
[1] "x" "y"
\$class
[1] "data.frame"
\$row.names
[1] 123


\section*{Data frames and tibbles}
- A data frame has a constraint: the length of each of its vectors must be the same.
■ A data frame has rownames () and colnames(). The names() of a data frame are the column names.
- A data frame has nrow() rows and ncol() columns. The length() of a data frame gives the number of columns.

\section*{Tibbles}
- Modern reimagining of the data frame.

■ tibbles are "lazy and surly": they do less and complain more.
```

library(tibble)
df2 <- tibble(x = 1:3, y = letters[1:3])
typeof(df2)
[1] "list"
attributes(df2)
\$class
[1] "tbl_df" "tbl" "data.frame"
\$row.names
[1] 1 2 3

## Creating data frames and tibbles

names(data.frame(`1` = 1))
[1] "X1"
names(tibble(`1` = 1))
[1] "1"

## Creating data frames and tibbles

```
data.frame(x = 1:4, y = 1:2)
    x y
1 1 1
2 2 2
3 3 1
4 2
```

```
tibble(x = 1:4, y = 1:2)
```

tibble(x = 1:4, y = 1:2)
Error in `tibble()`:
Error in `tibble()`:
! Tibble columns must have compatible sizes.
! Tibble columns must have compatible sizes.

* Size 4: Existing data.
* Size 4: Existing data.
* Size 2: Column `y`.
* Size 2: Column `y`.
i Only values of size one are recycled.

```
i Only values of size one are recycled.
```


## Creating data frames and tibbles

```
tibble(
    x = 1:3,
    y = x * 2,
    z = 5
)
# A tibble: 3 x 3
\begin{tabular}{rrr} 
<int> & <dbl> & <dbl> \\
1 & 2 & 5 \\
2 & 4 & 5 \\
3 & 6 & 5
\end{tabular}
```


## Row names

## Data frames allow you to label each row with a name, a character vector containing only unique values:

```
df3 <- data.frame(
    age = c(35, 27, 18),
)
df3
    age hair
Bob 35 blond
Susan 27 brown
Sam 18 black
```

    hair \(=c(" b l o n d ", ~ " b r o w n ", ~ " b l a c k ")\),
    row.names = c("Bob", "Susan", "Sam")
    
## Row names

- tibbles do not support row names
- convert row names into a regular column with either rownames_to_column (), or the rownames argument:

```
as_tibble(df3, rownames = "name")
```

\# A tibble: $3 \times 3$
name age hair
<chr> <dbl> <chr>
1 Bob 35 blond
2 Susan 27 brown
3 Sam 18 black

## Printing

dplyr::starwars

```
# A tibble: 87 x 14
    name height mass hair_color skin_color eye_color birth_year sex
    <chr> <int> <dbl> <chr> <chr> <chr> <dbl> <chr>
    1 Luke Skyw~
                            172
    2 C-3PO 167
    3 R2-D2 96
    4 \text { Darth Vad~ } 2 0 2
    5 Leia Orga~ 150
    6 \text { Owen Lars 178}
    7 \text { Beru Whit~ } 1 6 5
    8 R5-D4 97
    9 Biggs Dar~ 183
10 Obi-Wan K~ 182
# i 77 more rows
# i 6 more variables: gender <chr>, homeworld <chr>, species <chr>,
# films <list>, vehicles <list>, starships <list>
```


## Printing

- Tibbles only show first 10 rows and all columns that fit on screen. Additional columns shown at bottom.
■ Each column labelled with its type, abbreviated to 3-4 letters.
- Wide columns truncated.


## List columns

```
df <- data.frame(x = 1:3)
df$y <- list(1:2, 1:3, 1:4)
data.frame(
    x = 1:3,
    y = I(list(1:2, 1:3, 1:4))
)
\begin{tabular}{lllll} 
& \(x\) & & & \(y\) \\
1 & 1 & & 1, & 2 \\
2 & 2 & & 1, & 2, \\
3 & 3 & 1, & 2, & 3, \\
\hline
\end{tabular}
```



```
tibble(
    x = 1:3,
    y = list(1:2, 1:3, 1:4)
)
```


## Matrix and data frame columns

```
dfm <- tibble(
    x = 1:3 * 10,
    y = matrix(1:9, nrow = 3),
    z = data.frame(a = 3:1, b = letters[1:3])
)
str(dfm)
```

| x | y |  |  | z |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
|  |  |  |  | a | b |
| 10 | 1 | 4 | 7 | 3 | "a" |
| 20 | 2 | 5 | 8 | 2 | "b" |
| 30 | 3 | 6 | 9 | 1 | "c" |

tibble [3 x 3] (S3: tbl_df/tbl/data.frame)
\$ x: num [1:3] 10 2030
\$ y: int [1:3, 1:3] 123456789
\$ z:'data.frame': 3 obs. of 2 variables:
.. $\$$ a: int [1:3] 321
..\$ b: chr [1:3] "a" "b" "c"

## Exercises

${ }^{13}$ Can you have a data frame with zero rows? What about zero columns?
What happens if you attempt to set rownames that are not unique?
15
If df is a data frame, what can you say about $t(d f)$, and $t(t(d f))$ ? Perform some experiments, making sure to try different column types.
What does as.matrix() do when applied to a data frame with columns of different types? How does it differ from data.matrix()?

## NULL

length (NULL)
[1] 0
You can test for NULLs with is.null():

```
x <- NULL
x == NULL
```

logical(0)
is.null(x)
[1] TRUE

